

# e A Collective Effects at an EIC:

EMC effect, shadowing and anti-shadowing

V. Guzey talk

Gerald A. Miller

University of Washington

What was known in 2012

What happened since

The future -what can be done with an EIC

RMP with [Or Hen](#), Eli Piasetzky, Larry Weinstein  
[here](#)

Will focus on  $0.3 < x < 0.7$  Remarkable experimental progress  
Even though at high  $x$ , this work has implications for the EIC

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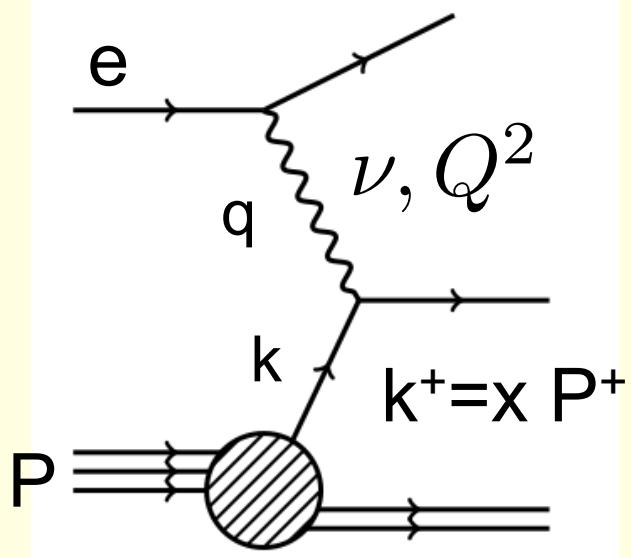
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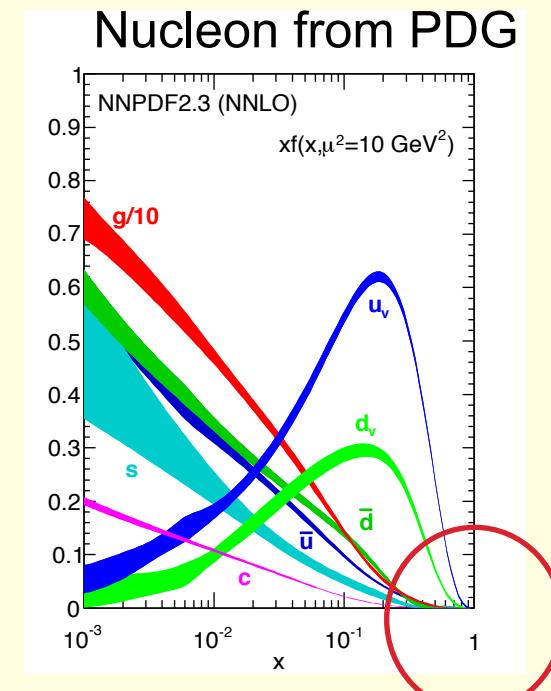
# Deep Inelastic Scattering



$$x = \frac{Q^2}{2P \cdot q} = \frac{k^0 + k^3}{P^0 + P^3} = \frac{k^+}{P^+}$$

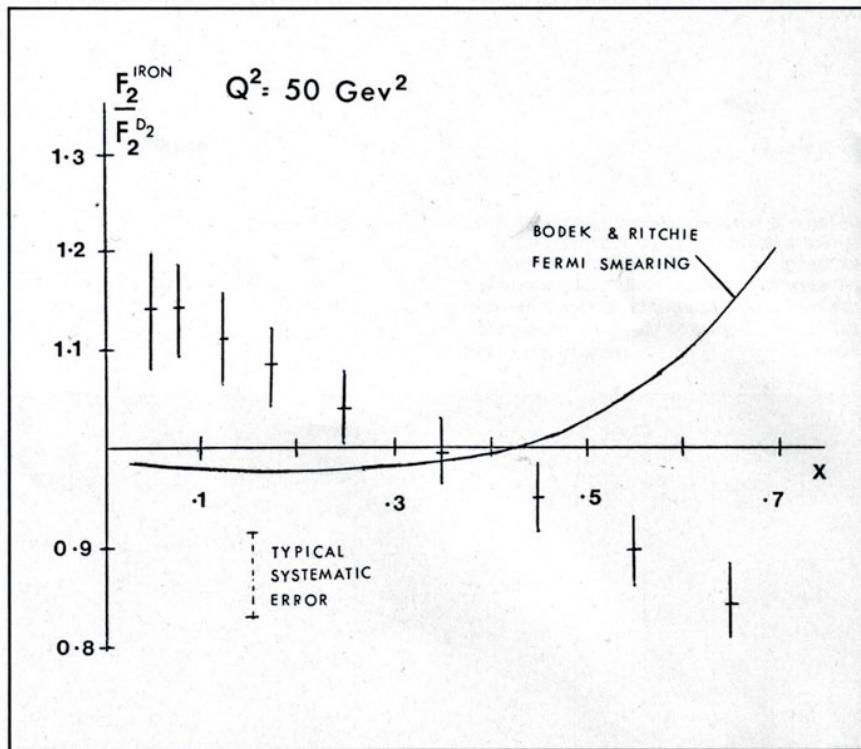
The 1982 EMC effect involves deep inelastic scattering from nuclei

EMC= European Muon Collaboration



# The EMC Effect

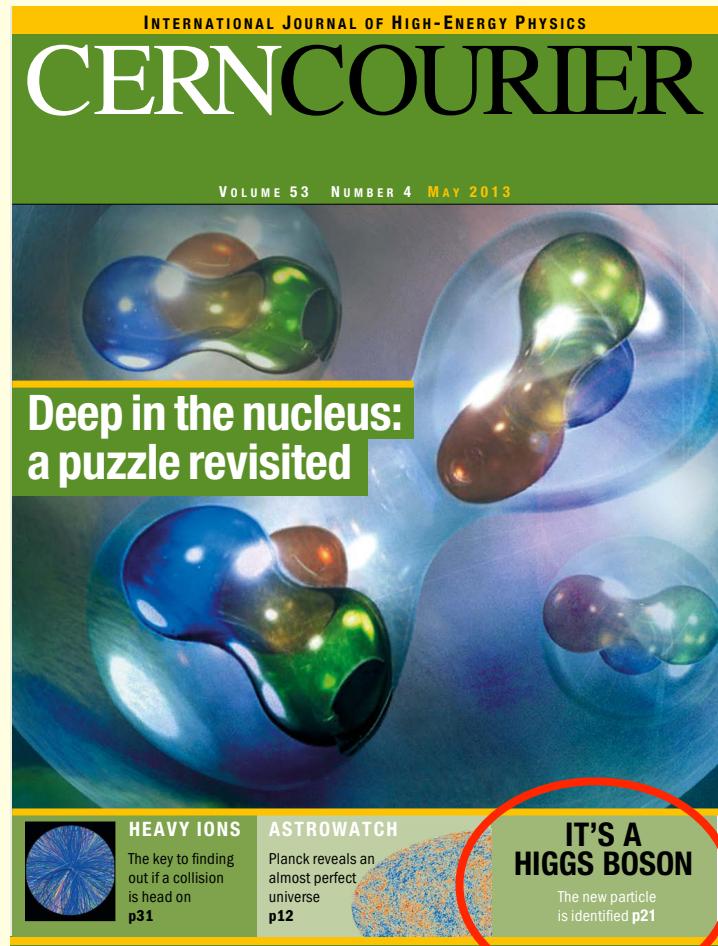
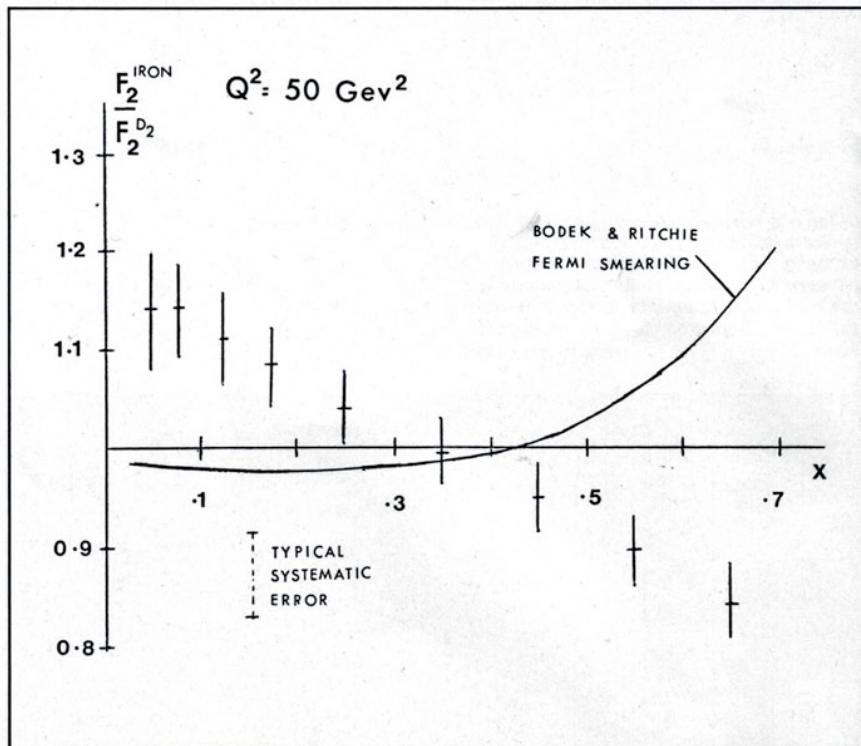
Cern Courier  
Nov. 1982



Higinbotham, Miller, Hen, Rith  
CERN Courier 53N4('13)24

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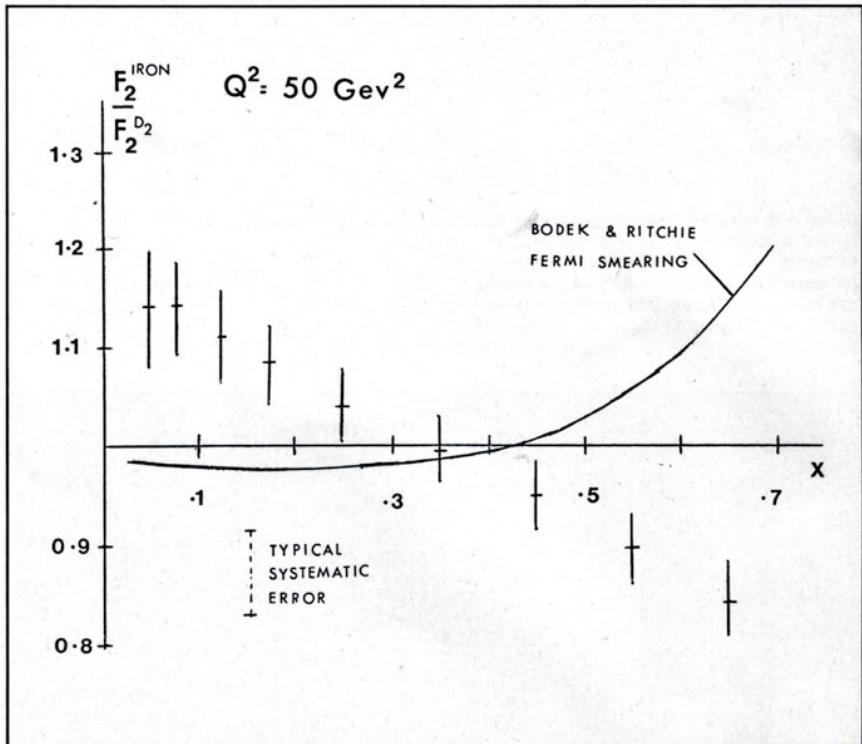
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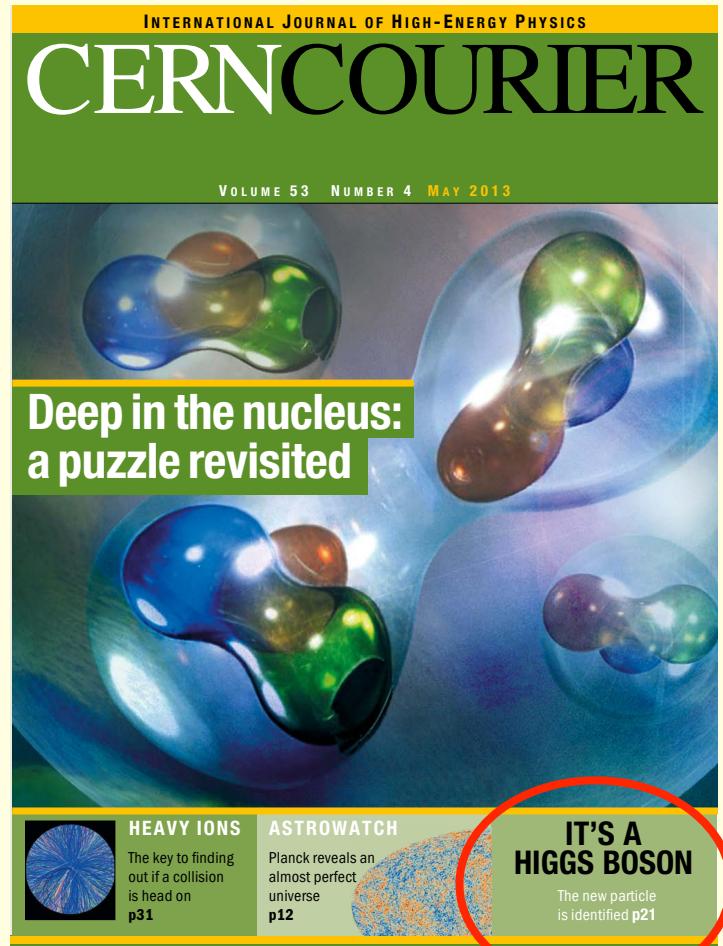
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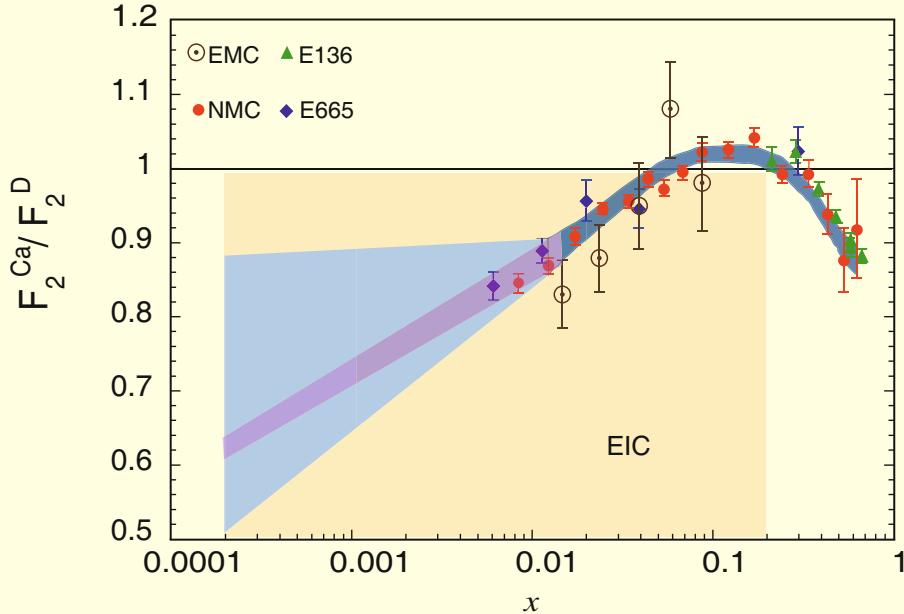
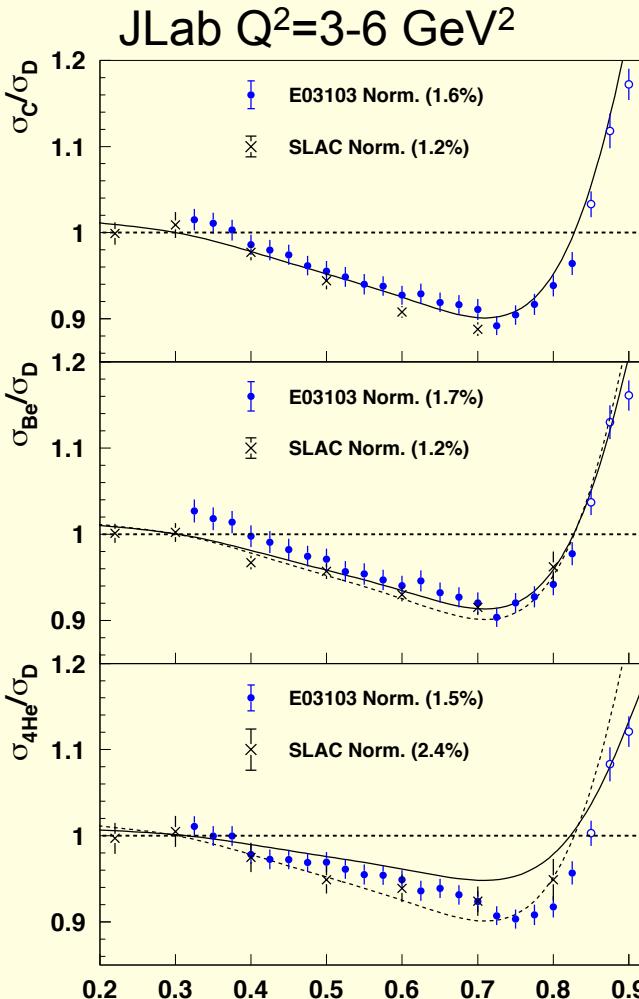


How does the nucleus emerge from QCD, a theory of quarks and gluons?



Higinbotham, Miller, Hen, Rith  
CERN Courier 53N4('13)24

# The EMC EFFECT



White Paper

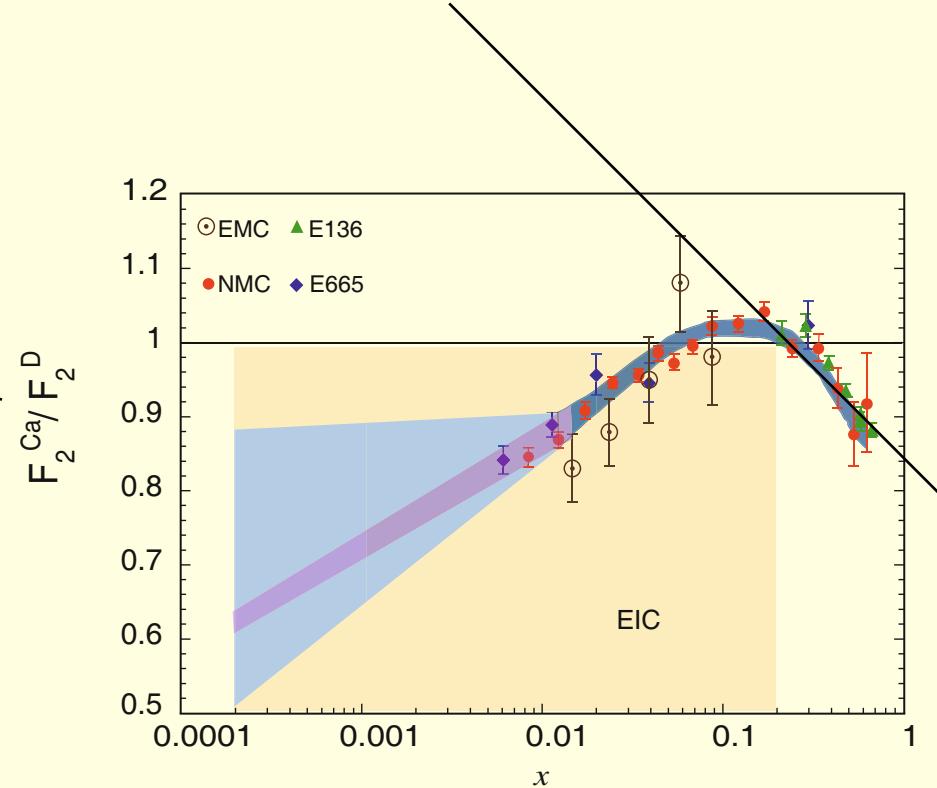
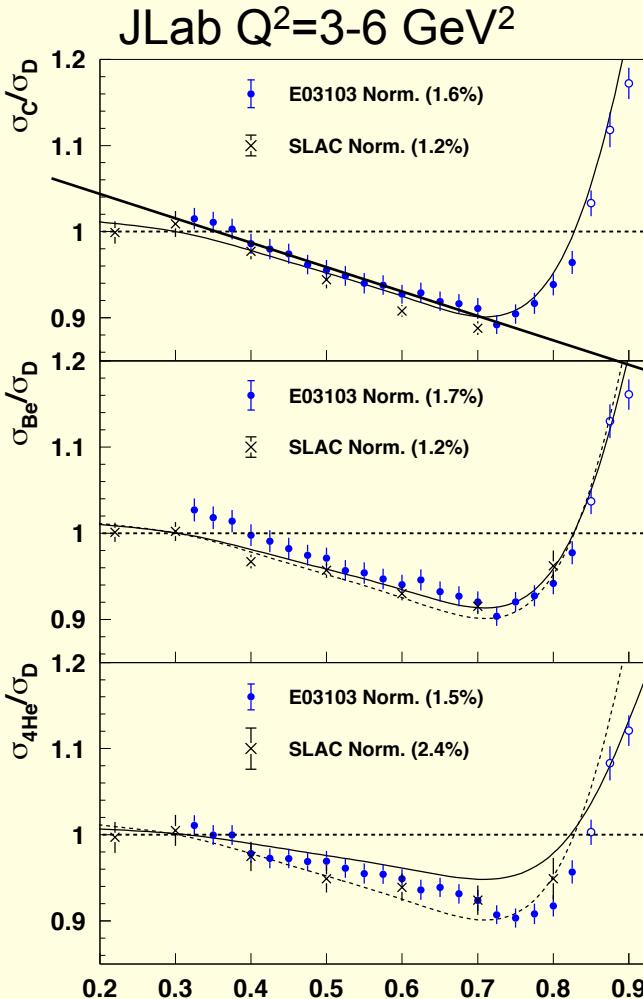
For  $0.3 < x < 0.7$  ratio =  $R^x$  is linear

Nucleon structure is modified: valence quark momentum depleted.

EFFECTS ARE SMALL ~15%

Why are ratios independent  
of  $Q^2$ ?<sup>4</sup>

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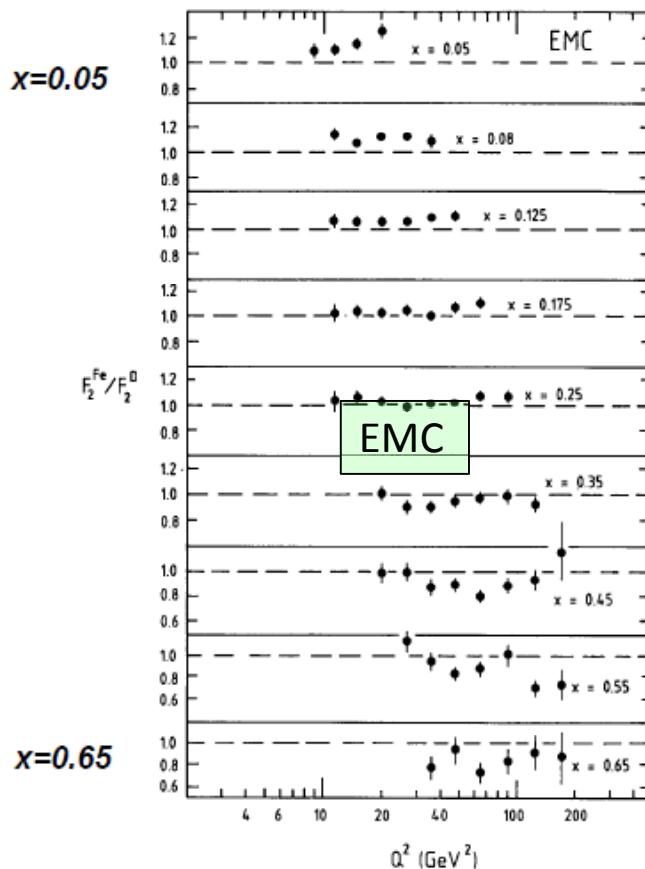
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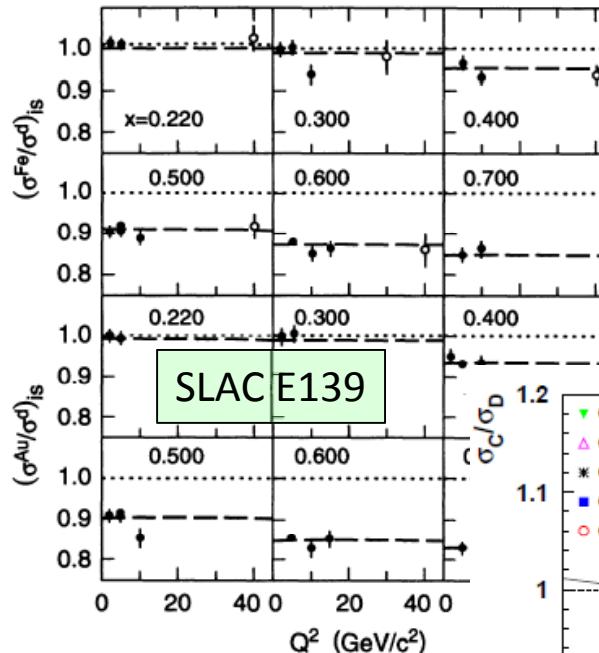
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# $Q^2$ dependence of nuclear effects

J.J. Aubert et al.,  
Nucl. Phys. B 481 (1996) 23

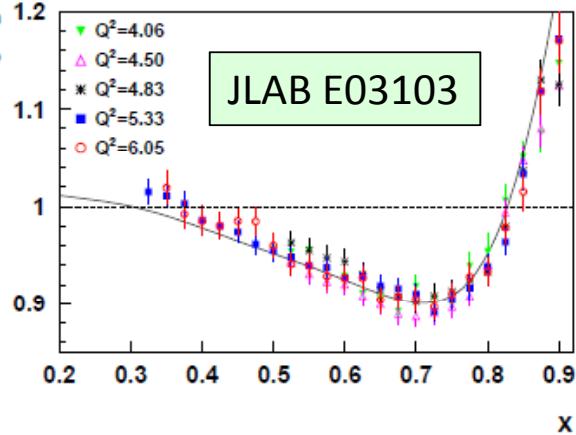


J. Gomez et al.,  
PRD 49 (1994) 4348



Klaus Rith

J. Seely et al.,  
PRL 103 (2009) 202301



$Q^2$  dependence of EMC effect is small

Why?

# Ideas: ~1000 papers 3 ideas

- Proper treatment of known effects: binding, Fermi motion, pionic- NO nuclear modification of internal nucleon/pion quark structure
- Quark based- high momentum suppression implies larger confinement volume
  - a bound nucleon is larger than free one- a mean field effect
  - b multi-nucleon clusters - beyond the mean field

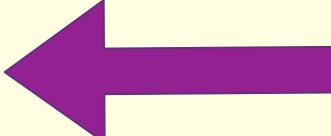
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**EMC – “Everyone’s Model is Cool (1985)”**

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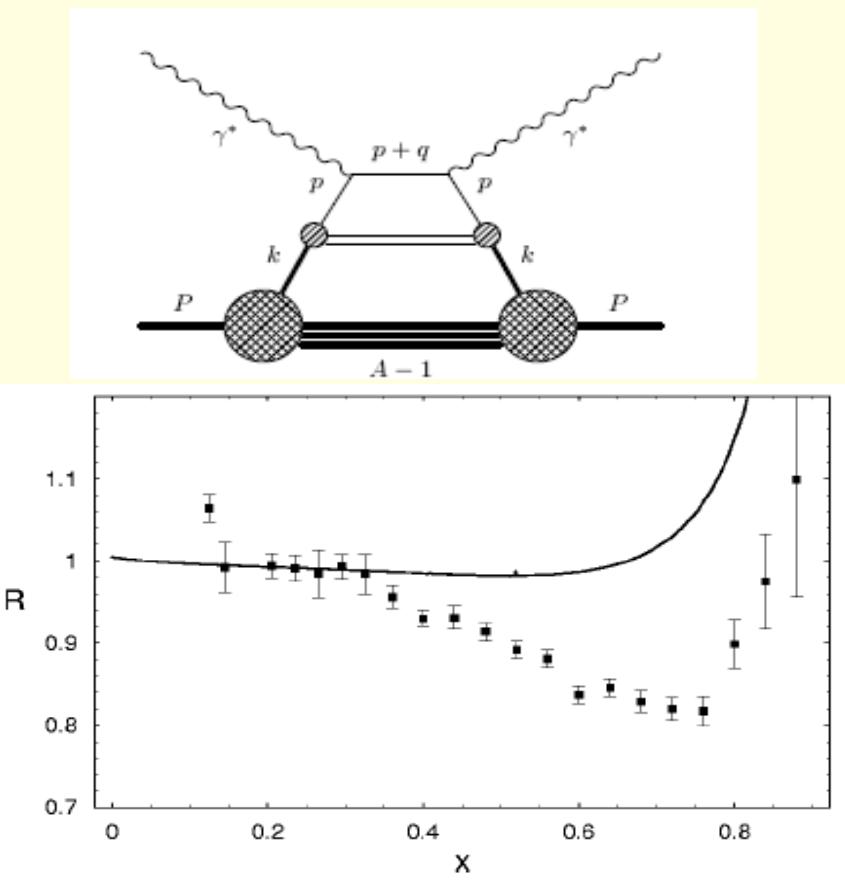
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EMC – “Everyone’s Model is Cool (1985)”

# One thing I learned since '85

- Nucleon/pion model is not cool  
Deep Inelastic scattering from nuclei-  
nucleons only free structure function
  - Hugenholtz van Hove theorem nuclear stability implies (in rest frame)  $P^+ = P^- = M_A$
  - $P^+ = A(M_N - 8 \text{ MeV})$
  - average nucleon  $k^+$   
 $k^+ = M_N - 8 \text{ MeV}$ , Not much spread
  - $F_{2A}/A \sim F_{2N}$  no EMC effect



Binding causes no EMC effect

Momentum sum rule-  
matrix element of energy  
momentum tensor

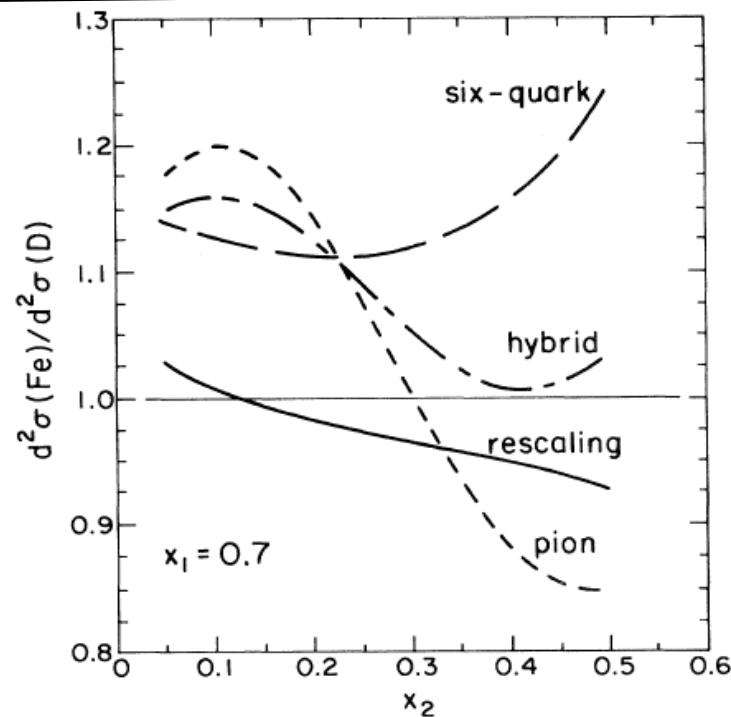
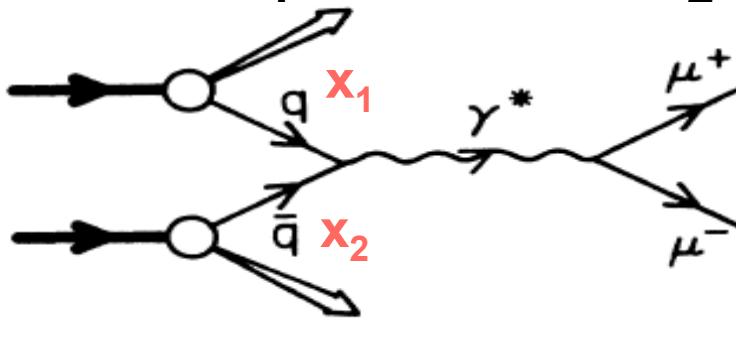
# Nucleons and pions

$$P_A^+ = P_N^+ + P_\pi^+ = M_A$$

$P_\pi^+/M_A = .04$ , explain EMC, sea enhanced

try Drell-Yan, Bickerstaff, Birse, Miller 84

proton( $x_1$ ) nucleus( $x_2$ )



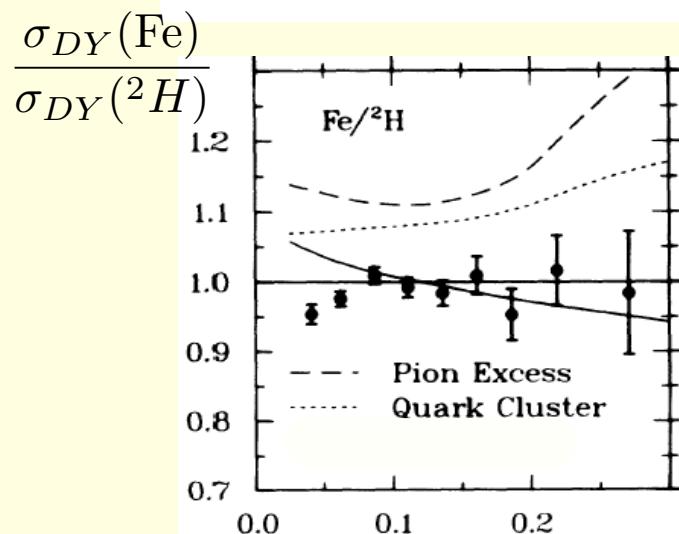
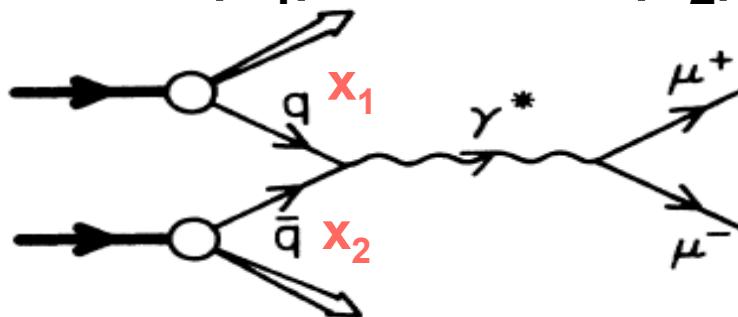
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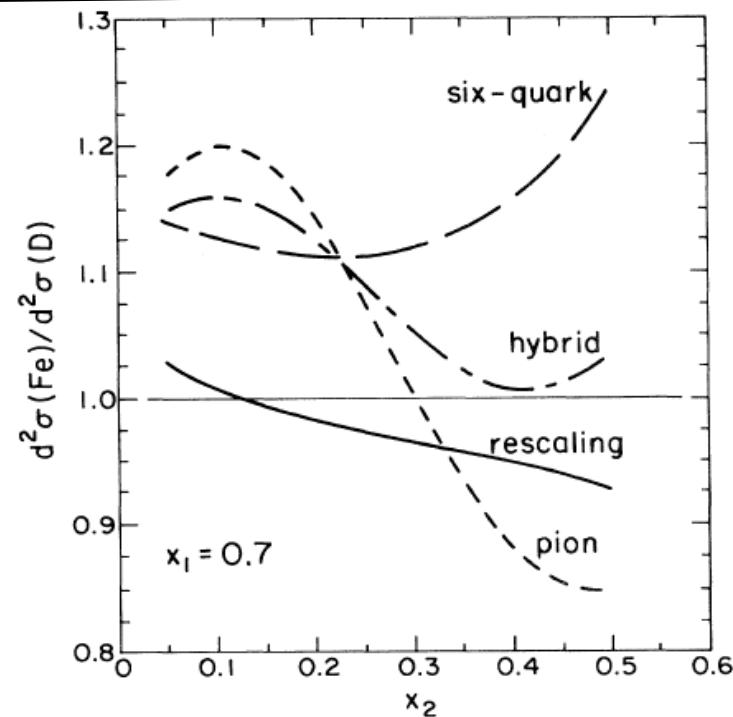
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E772 PRL 69, 1726 (92)



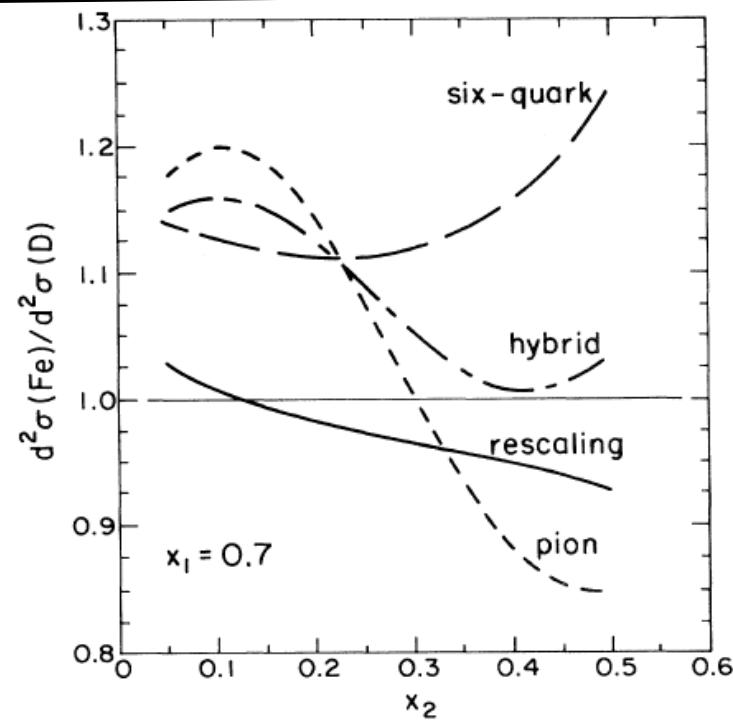
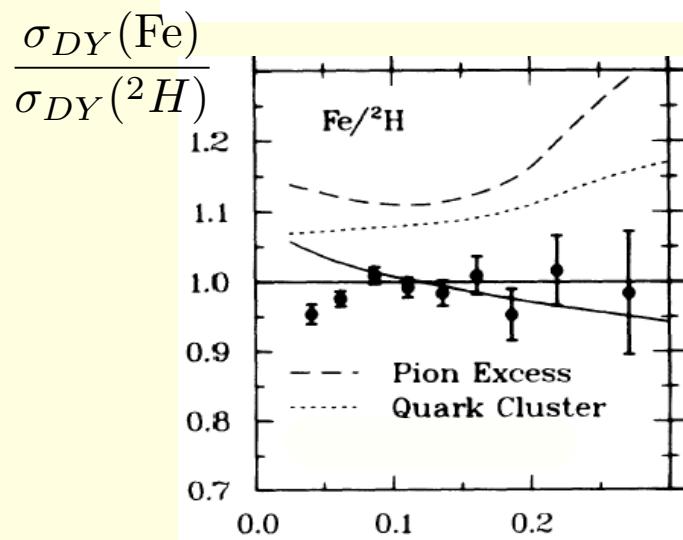
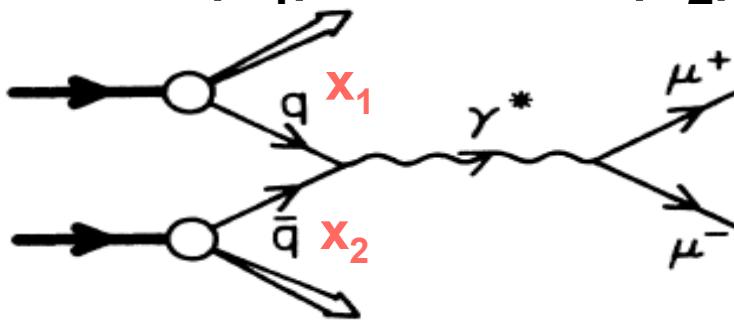
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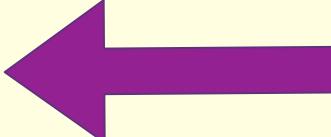
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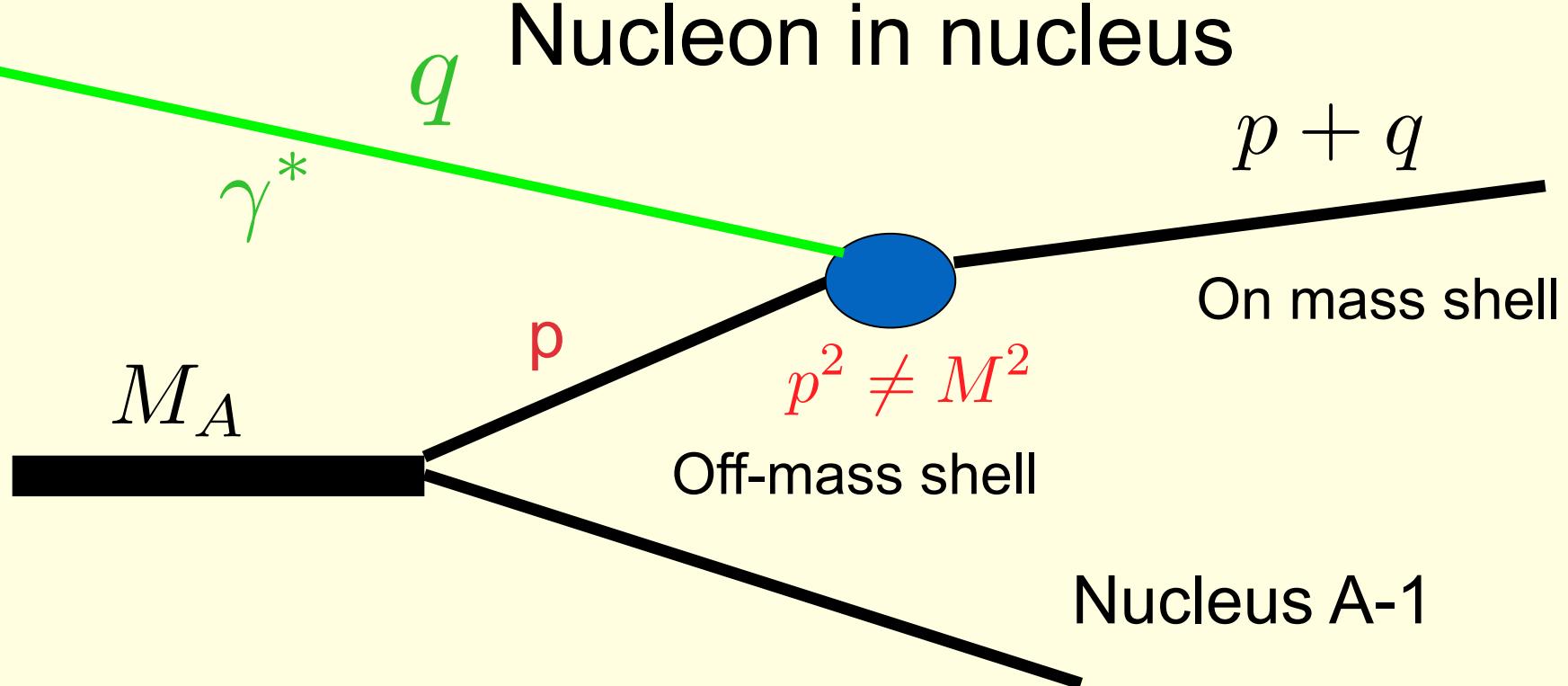


Bertsch, Frankfurt, Strikman “crisis”

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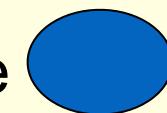
# Nucleon in nucleus



Nucleus A-1

is form factor of  
“large” proton

a A-1 nucleus is low-lying state



b A- nucleus is 1 fast nucleon +A-2 nucleus  
the struck nucleon is part of correlated pair SRC

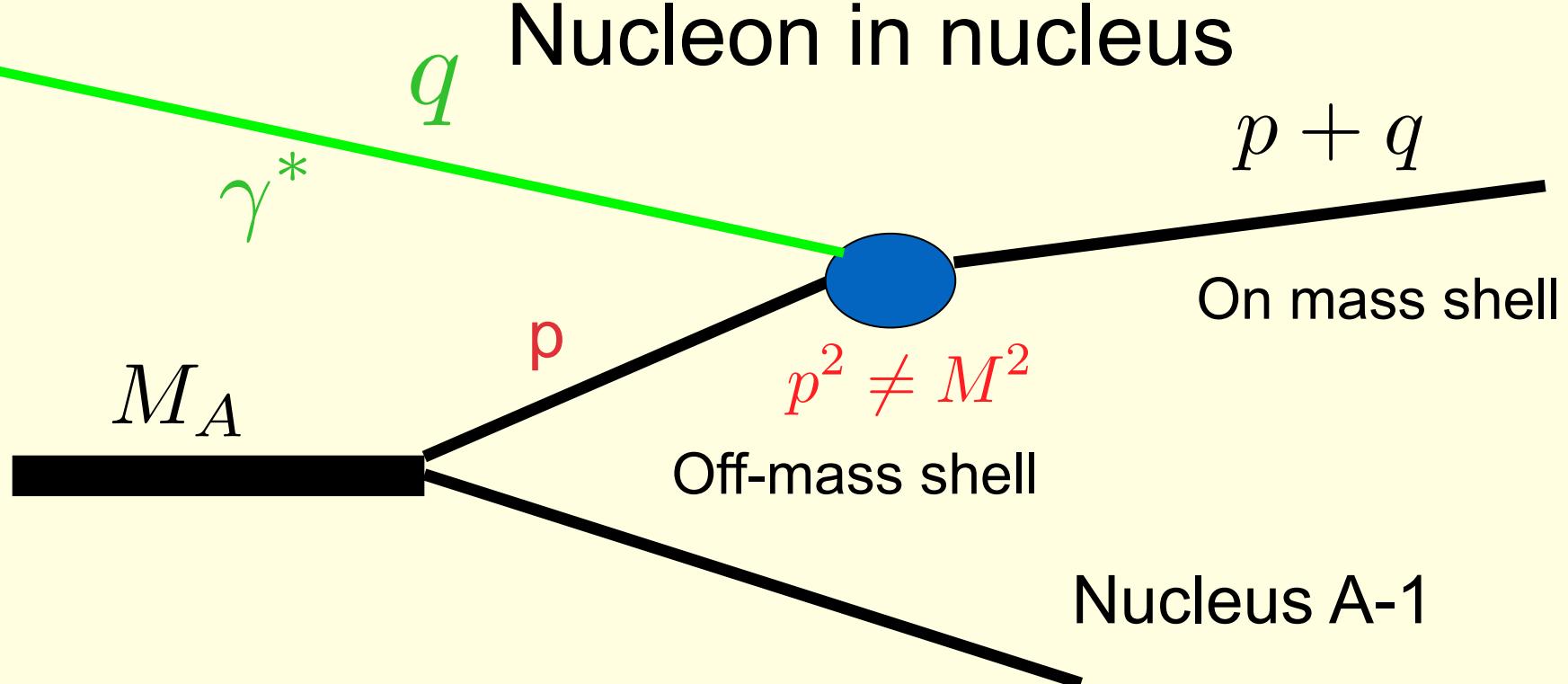
If Nucleus A-1 is highly excited, then

$$p^2 - M^2$$

is big

Such large virtuality occurs from two nearby correlated nucleons  
Highly virtually nucleon is not a nucleon- different quark config.

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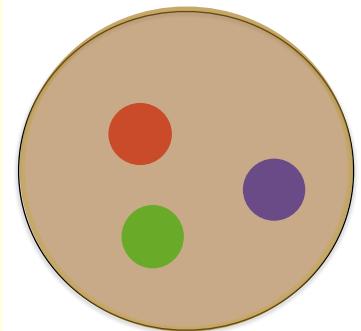
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# Quark structure of nucleon

Frankfurt-  
Strikman

BLC



PLC

+  $\epsilon$



gives high x  
 $q(x)$

PLC does not  
interact with  
nucleus

Schematic two-component nucleon model:  
Blob-like config: BLC  
Point-like config: PLC

$$\text{Free nucleon : } H_0 = \begin{bmatrix} E_B & V \\ V & E_P \end{bmatrix}, V > 0$$

$$|N\rangle = |B\rangle + \epsilon|P\rangle, \epsilon = \frac{V}{E_B - E_P} < 0$$

$$\text{In nucleus (M) : } H = \begin{bmatrix} E_B - |U| & V \\ V & E_P \end{bmatrix}$$

$|N\rangle_M = |B\rangle + \epsilon_M|P\rangle, |\epsilon_M| < |\epsilon|$ , PLC suppressed,  $\epsilon_M - \epsilon > 0$  amplitude effect!

$$|N\rangle_M - |N\rangle \propto (\epsilon_M - \epsilon) \propto U = \frac{p^2 - m^2}{2M} \text{ Shroedinger eq.}$$

$$q_M(x) = q(x) + (\epsilon_M - \epsilon)f(x)q(x), \frac{df}{dx} < 0, x \geq 0.3 \text{ PLC suppression}$$

$$R = \frac{q_M}{q}; \frac{dR}{dx} = (\epsilon_M - \epsilon) \frac{df}{dx} < 0 \text{ Reproduces EMC effect - like every model}$$

Why this model??? Large effect if  $v = p^2 - m^2$  is large, it is

Cioffi degli Atti '07

| A                       | $U = \langle v(\mathbf{p}, E) \rangle / 2M$ |
|-------------------------|---|
| $^3\text{H} = \text{e}$ | -34.59                                      |
| $^4\text{He}$           | -69.40                                      |
| $^{12}\text{C}$         | -82.28                                      |
| $^{16}\text{O}$         | -79.68                                      |
| $^{40}\text{Ca}$        | -84.54                                      |
| $^{56}\text{Fe}$        | -82.44                                      |
| $^{208}\text{Pb}$       | -92.20                                      |

large values from  
two nucleon  
correlations Simula

# Implication of model

The two state model has a ground state  $|N\rangle$  and an excited state  $|N^*\rangle$

$$|N\rangle_M = |N\rangle + (\epsilon_M - \epsilon)|N^*\rangle$$

The nucleus contains excited states of the nucleon

These configurations are the origin of high  $x$  EMC ratios

# $A(e,e')$ at $x>1$ shows dominance of 2N SRC

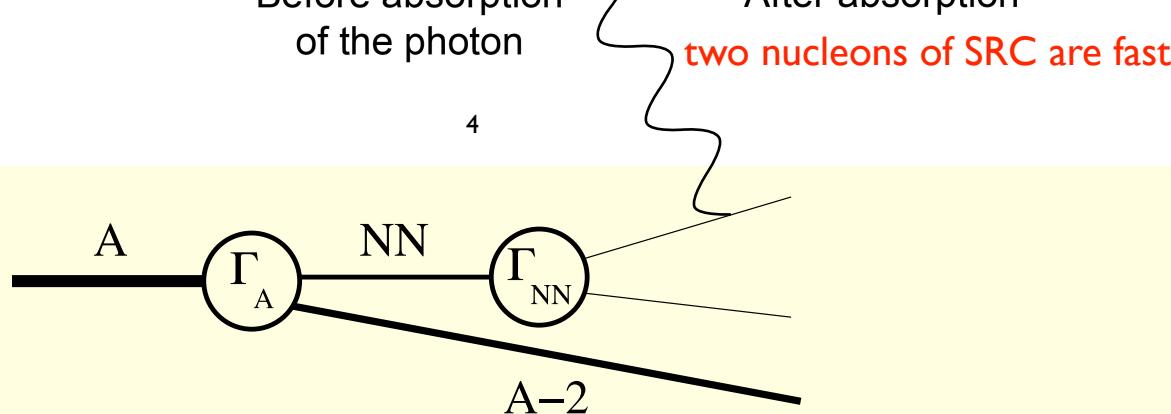
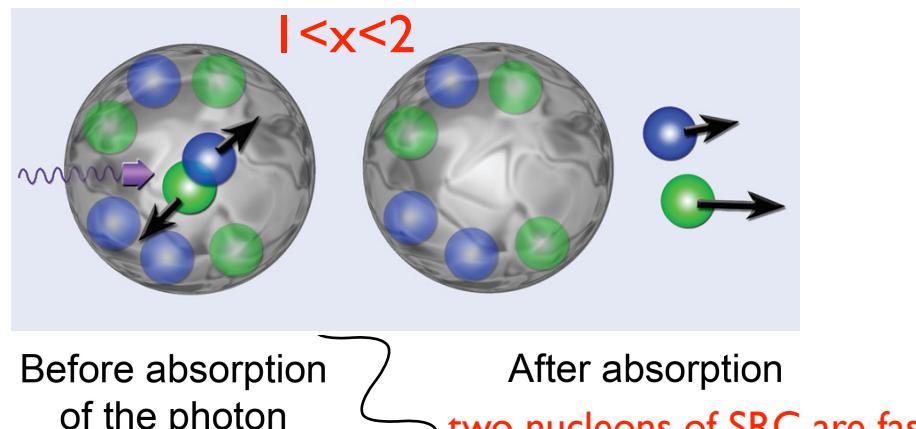
$$x = \frac{Q^2}{2M\nu}$$

$x$  goes from 1 to A

$x=1$  is **exact** kinematic limit **for all  $Q^2$**  for the scattering off a free nucleon;  
 $x=2$  ( $x=3$ ) is **exact** kinematic limit **for all  $Q^2$**  for the scattering off a  $A=2$ ( $A=3$ ) system (up to <1% correction due to nuclear binding)

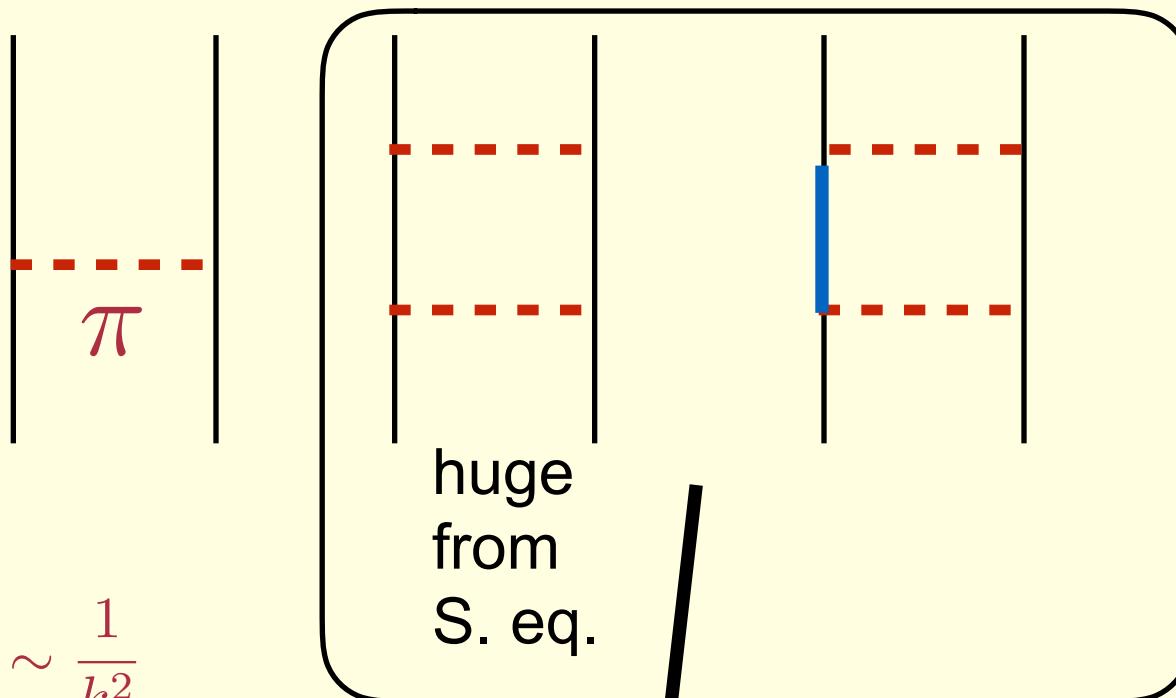
M Strikman  
picture

Two nucleons cluster



# How/why nucleons in nuclei cluster

one pion exchange between n and p



$$\psi(k) \sim \frac{1}{k^2}$$

$$300 \text{ MeV}/c < k < 500 \text{ MeV}/c$$

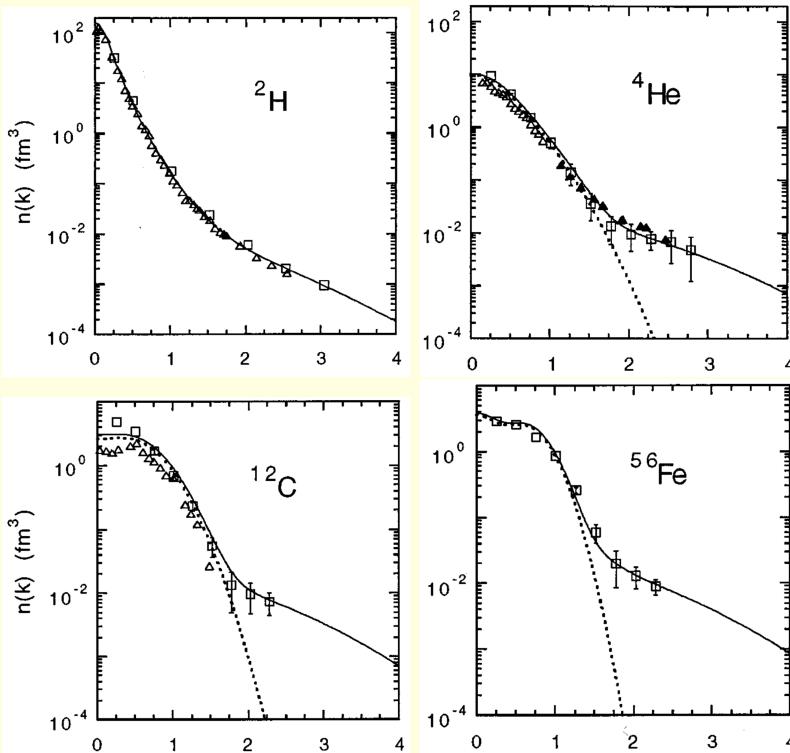
Supports high momentum transfer

Not effective range

Two nucleons are stuck/struck together

# Two nucleon correlations

$n(k)$



Chen et al '16

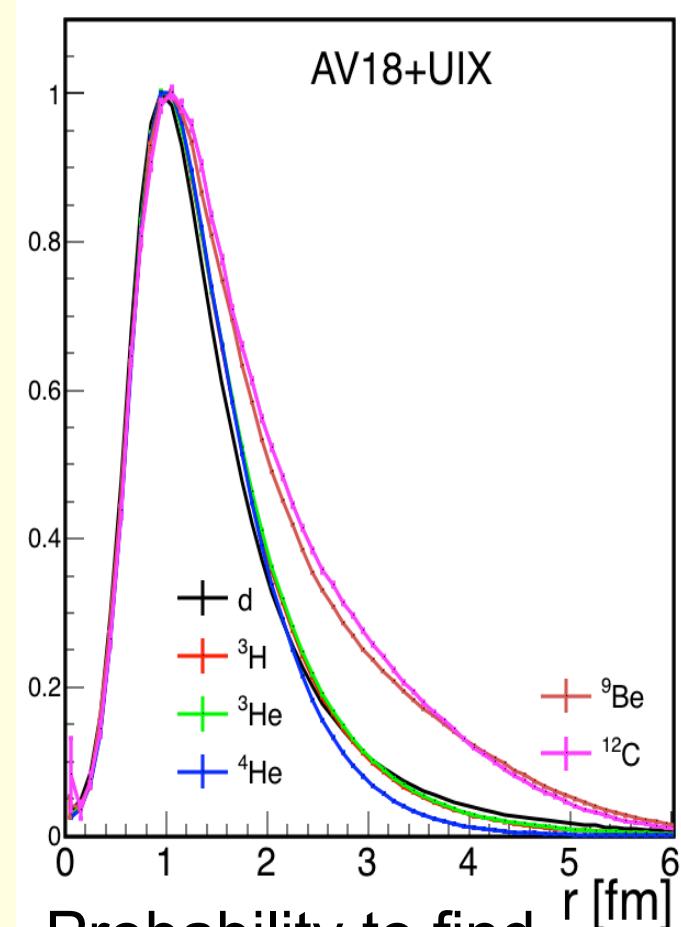


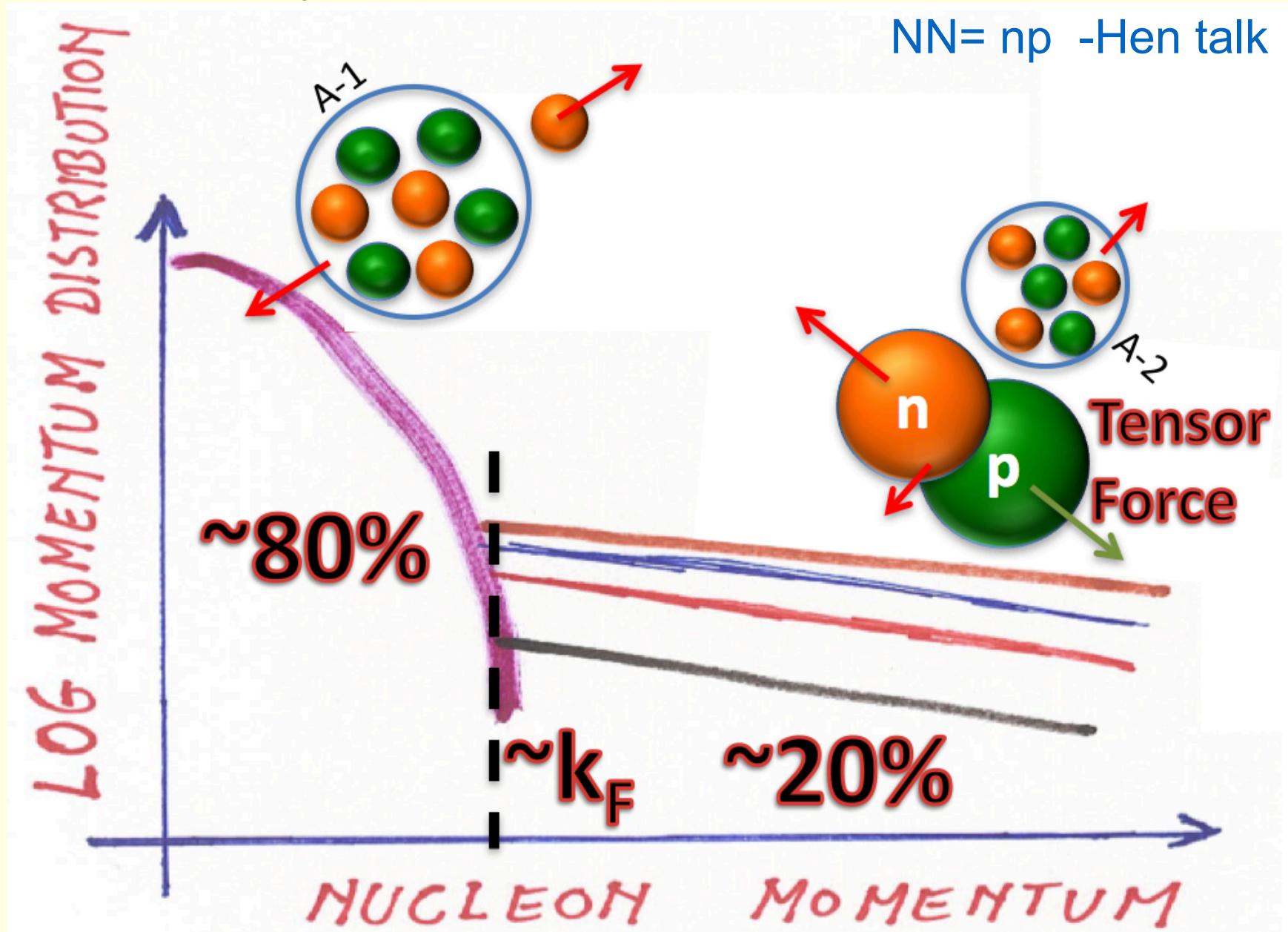
FIG. 4: The nucleon momentum distributions  $n_0(k)$  (dashed line) and  $n(k)$  (solid line) plotted versus momentum in  $\text{fm}^{-1}$  for the deuteron,  $^4\text{He}$ ,  $^{12}\text{C}$  and  $^{56}\text{Fe}$ . Figure adapted from (Ciofi degli Atti and Simula,

Probability to find  
nucleons separated  
by  $r$   
<sub>15</sub>

# Summary of Correlations

J Ryckebusch pic

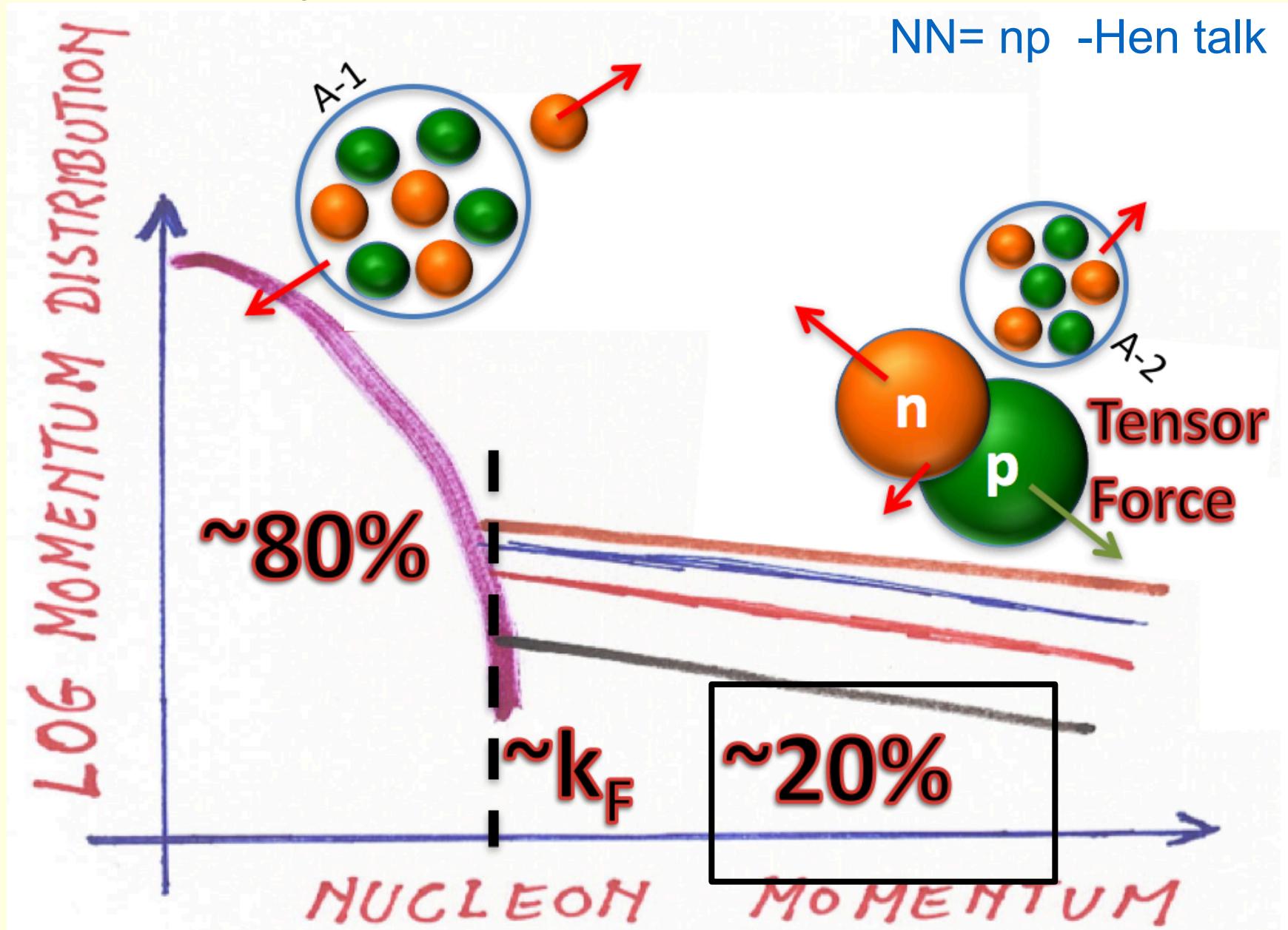
NN= np -Hen talk



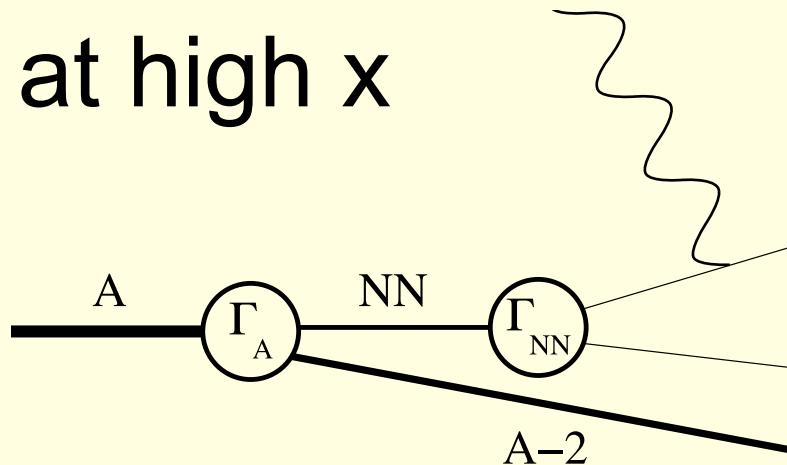
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(e,e') at high x

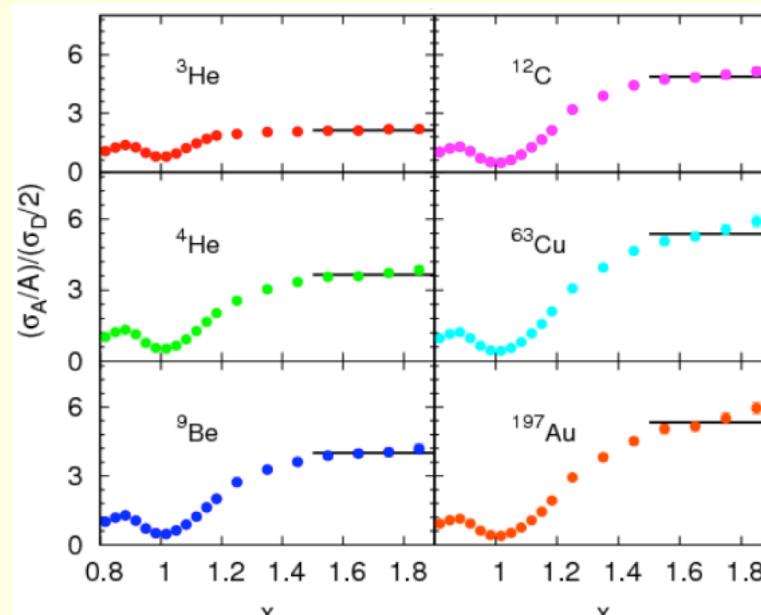
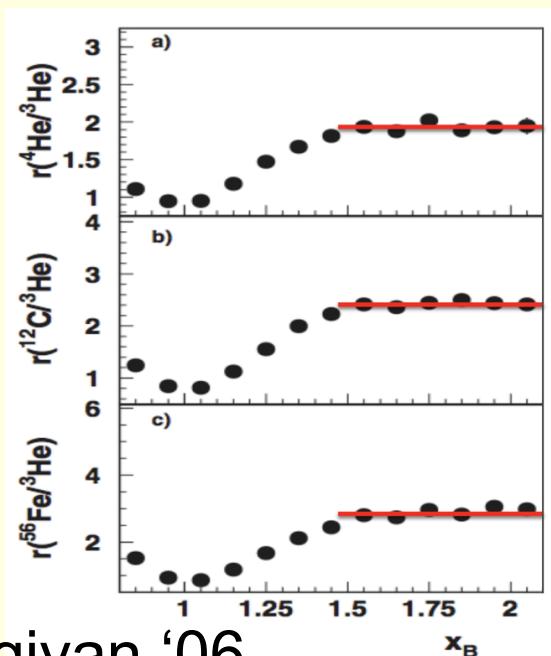


NN= np -Hen talk

$1 < x < 2$  leading term:

$$\frac{2}{A} \sigma(x, Q^2) \approx a_2(A) \sigma_2(x, Q^2) \approx a_2(A) \sigma_D(x, Q^2)$$

np dominance -Hen talk

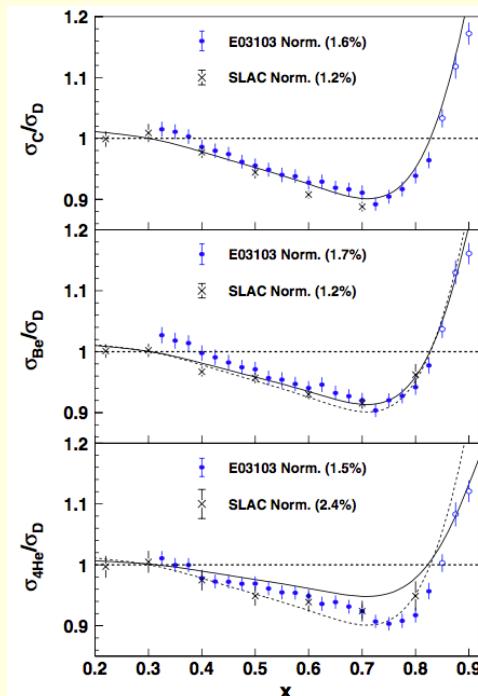


Fomin et al  
'11

$a_2$

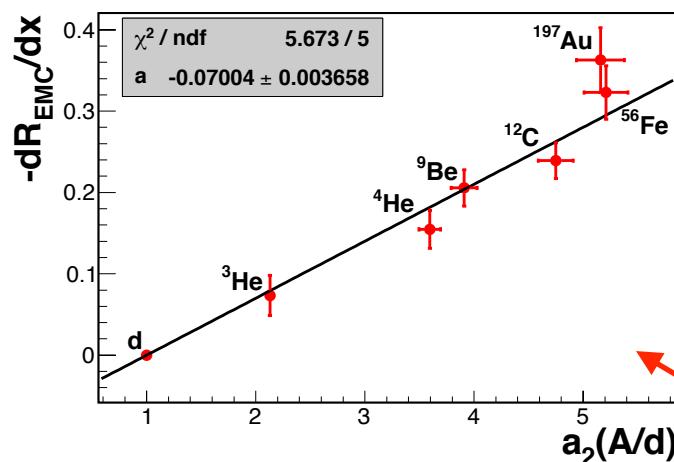
DIS

Hen et al 2013

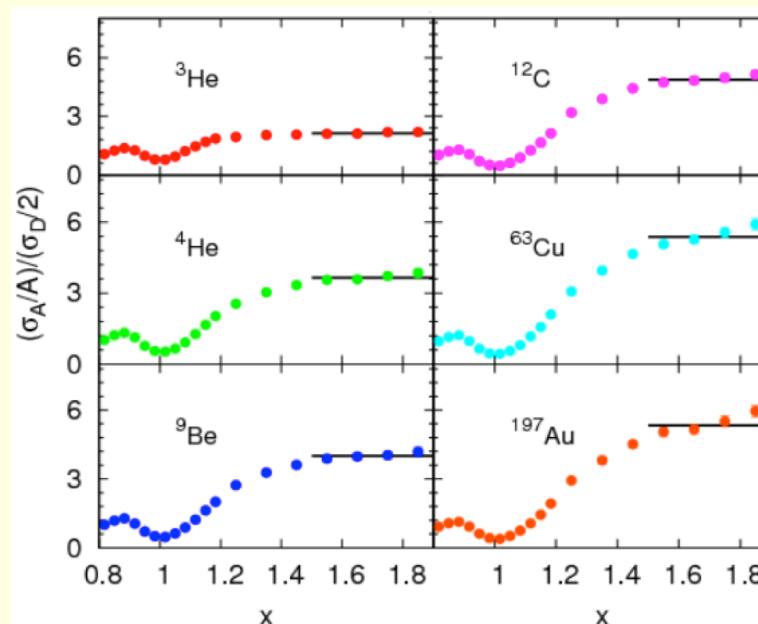


Seely et al 2009

get slope



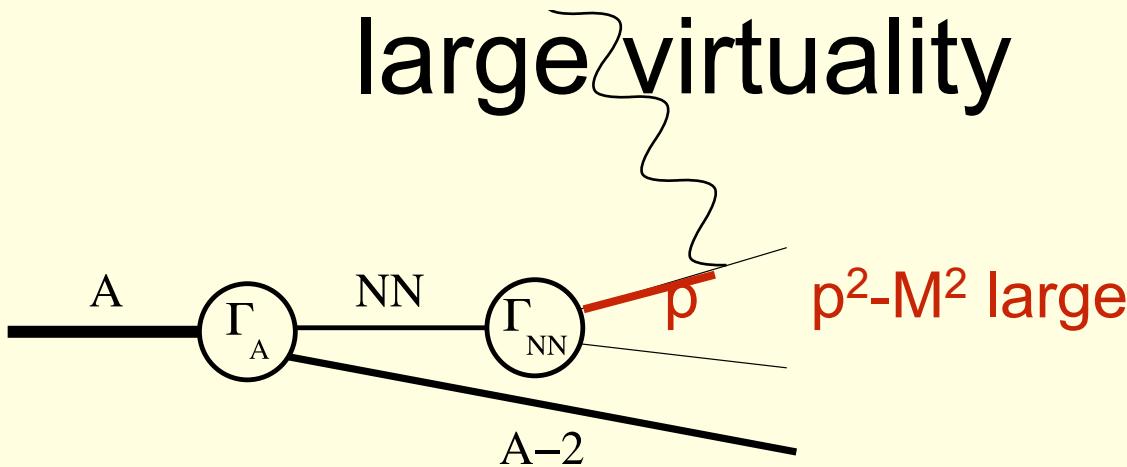
Linear relation  
accident?



Fomin et al  
2012  
 $\uparrow a_2$

18

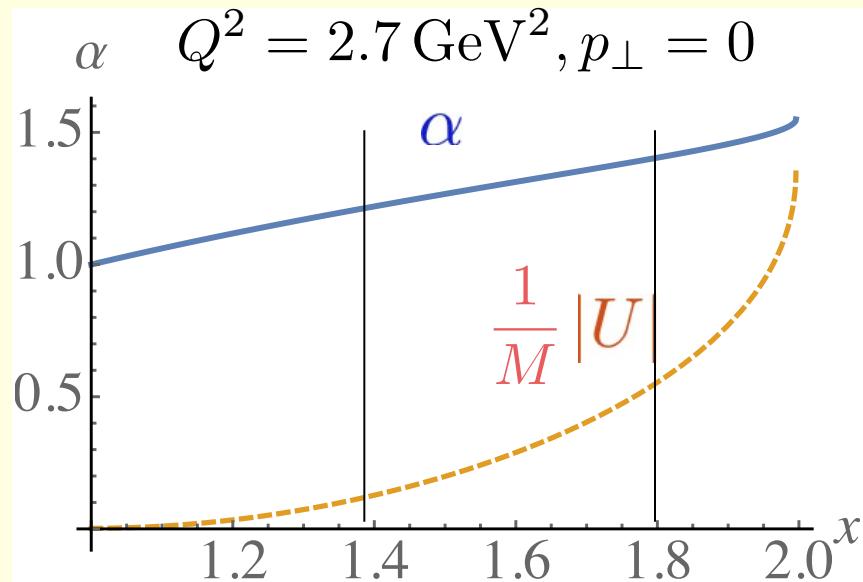
# Common cause of $dR/dx$ and $a_2(A)$ : large virtuality



Given  $Q^2$ ,  $x$ ,  $p_\perp$

4-momentum conservation determines  $2\frac{p^+}{P_D^+} \equiv \alpha$  and  $v = p^2 - M^2$

Sees wave function at  $\alpha \approx 1.2$



$|U|$  is large  $v$  is large  
can only get this from  
short range correlation

large  $v$  is responsible for  
both  $dR/dx$  and  $a_2(A)$

# Logic/Summary

|                              |  |                              |
|------------------------------|--|------------------------------|
| Data                         | DIS-large x<br>(e,e')  | Plateau large x<br>(e,e',NN) |
| Interpret:                   | valence quark<br>momentum<br>decrease in A                     | 2 baryon clusters            |
| QCD                          | nucleon wf has<br>BLC,PLC etc<br>PLC -high x<br>PLC suppressed |                              |
|                              |  | Large virtuality             |
| Short-ranged<br>interactions |  | np<br>dominance              |

# Logic/Summary

EMC effect and  
large x plateau  
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DIS-large x       $(e, e')$  Plateau large x       $(e, e', NN)$

Interpret:

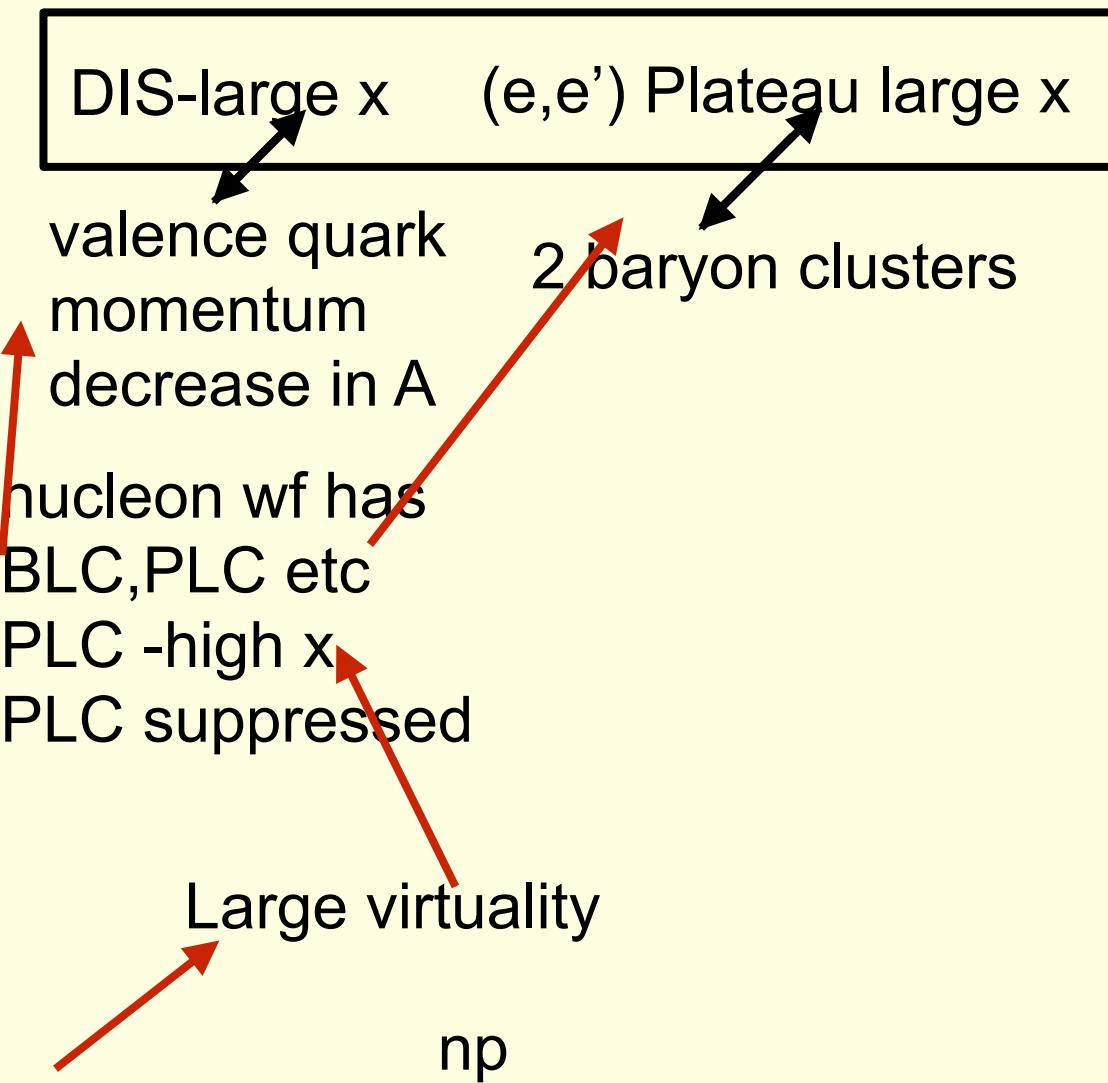
valence quark  
momentum  
decrease in A  
nucleon wf has  
BLC,PLC etc  
PLC -high x  
PLC suppressed

QCD

Large virtuality

Short-ranged  
interactions

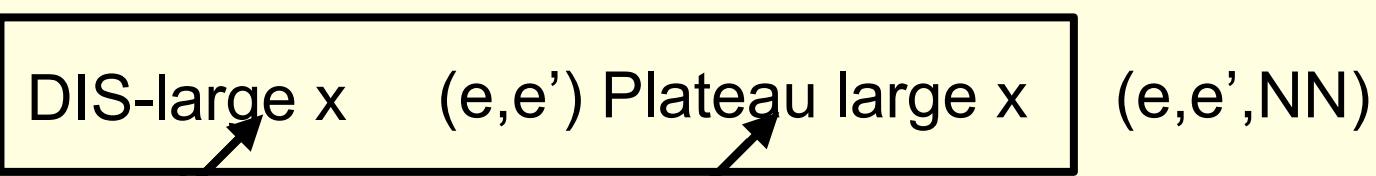
np  
dominance



# Logic/Summary

EMC effect and  
large x plateau  
have same cause

Data



Interpret:

QCD

Short-ranged  
interactions

valence quark  
momentum  
decrease in A

nucleon wf has  
BLC,PLC etc

PLC -high x  
PLC suppressed

2 baryon clusters

Large virtuality

np  
dominance

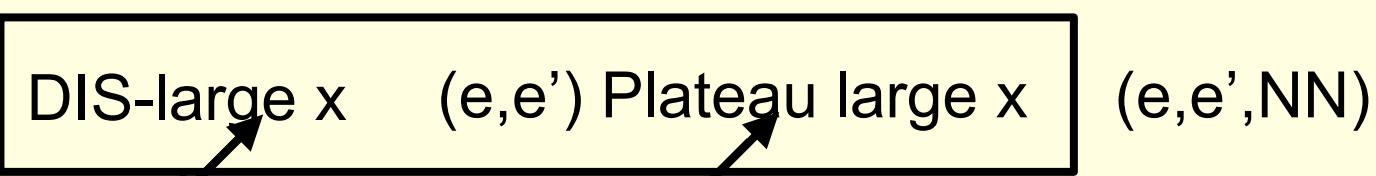
Large virtuality

np  
dominance

# Logic/Summary

EMC effect and  
large x plateau  
have same cause

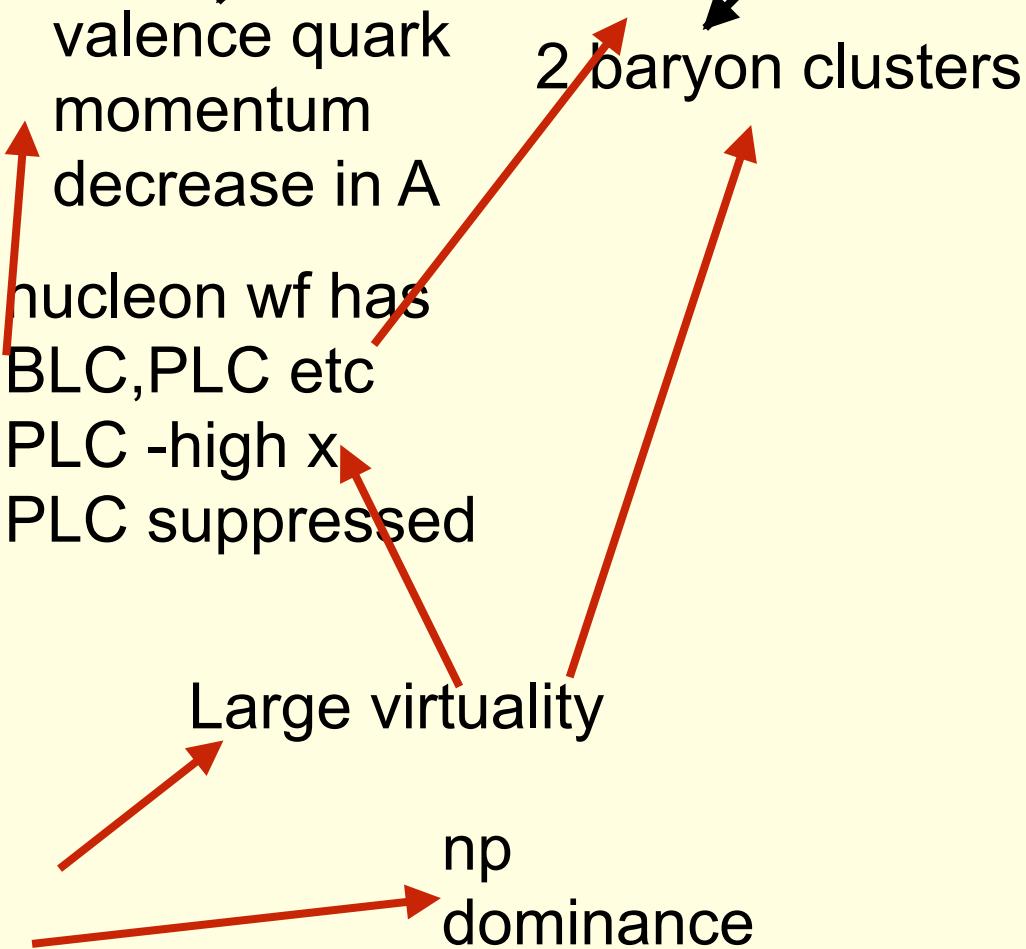
Data



Interpret:

QCD

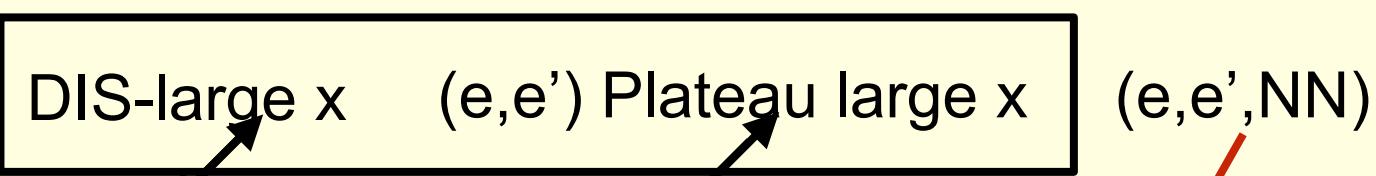
Short-ranged  
interactions



# Logic/Summary

EMC effect and  
large x plateau  
have same cause

Data



Interpret:

QCD

Short-ranged  
interactions

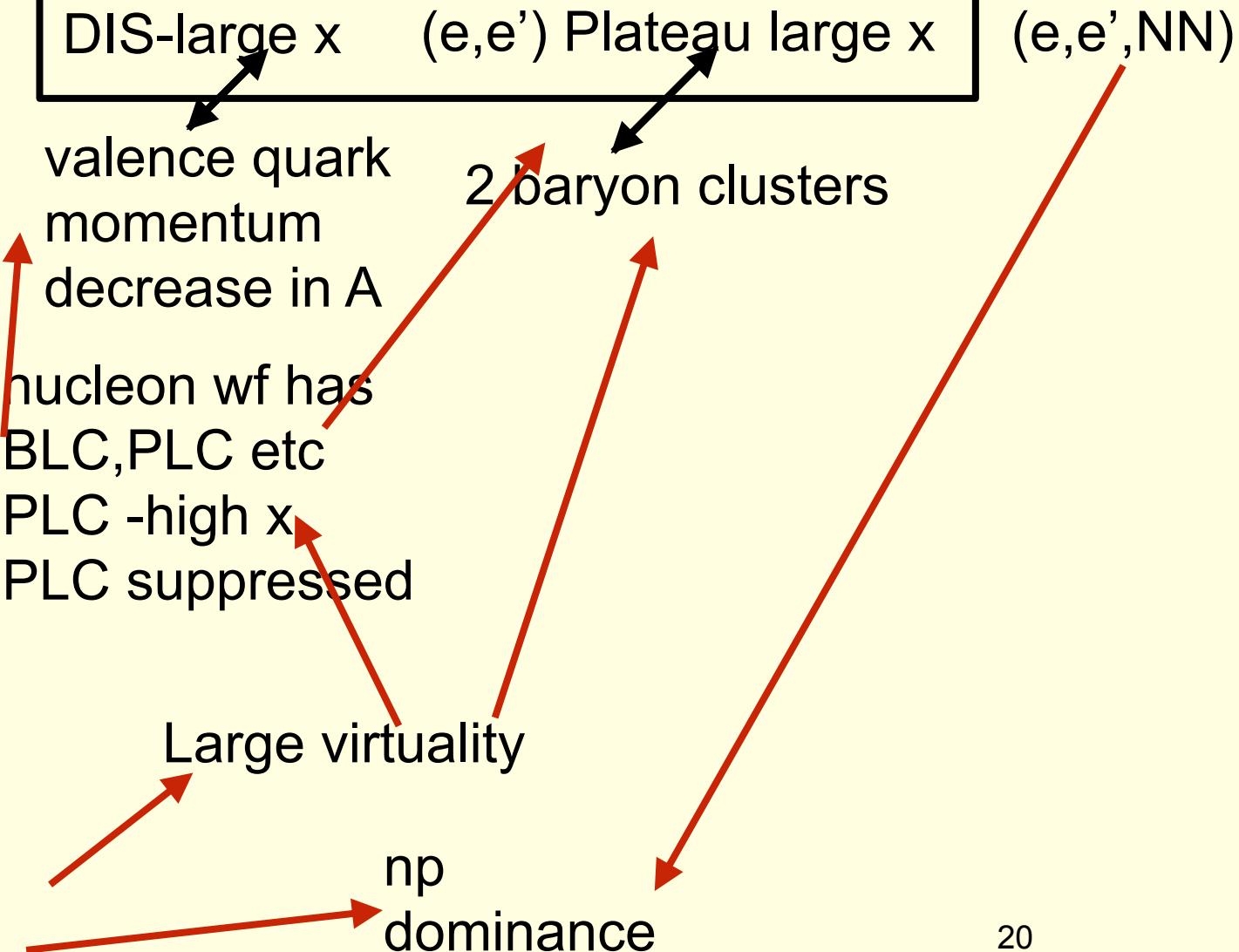
valence quark  
momentum  
decrease in A

nucleon wf has  
BLC,PLC etc

PLC -high x  
PLC suppressed

Large virtuality

np  
dominance



# Implications for nuclear physics

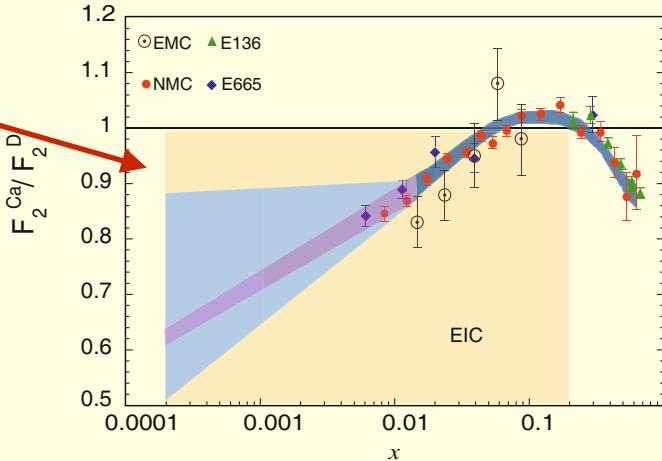
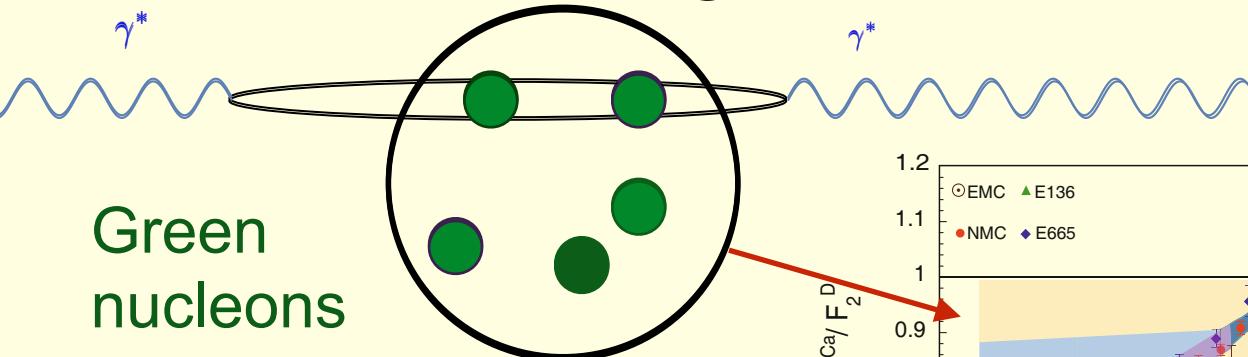
- Nucleus modifies nucleon electroweak form factors
- Nucleon excited states exist in nuclei
- Medium modifications in deuteron influence extracted neutron  $F_2$
- spectator tagging Cosyn talk

## Implication 1 for EIC?

### Why are EMC ratios independent of $Q^2$ ?

- Is the medium modification for matrix elements yielding higher-twist effects same as for leading twist? M. Strikman
- Can EIC add by examining  $Q^2$  dependence
- Large  $x$  is on the kinematic edge, but perhaps can do during a phase in which energy is ramped up<sup>22</sup>

# Shadowing & Anti-shadowing

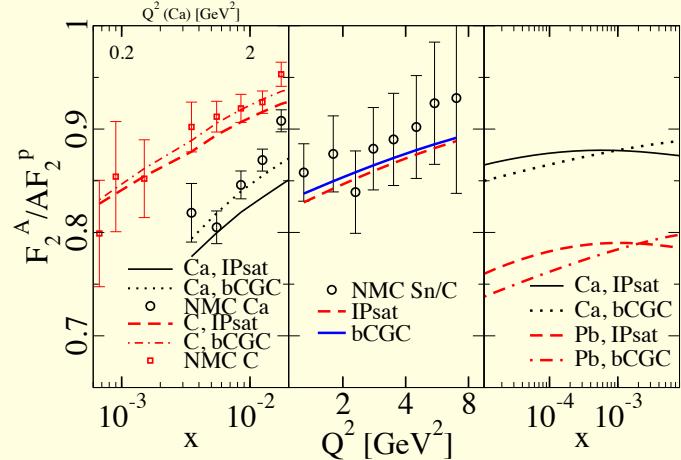


Frankfurt Strikman and Guzey

Physics Reports 512 (2012) 255–393

no parton saturation

Kowalski Lappi Venugopalan PRL 100, 022303 use CGC,  
gluon saturation; many recent papers & discussion of detailed models



But nuclear wave functions  
enter in **all** approaches



All approaches need two-nucleon density:  $\rho^{(2)}(\mathbf{r}_1, \mathbf{r}_2) \equiv \langle A | \sum_{i \neq j} \delta(\mathbf{r}_1 - \mathbf{r}_i) \delta(\mathbf{r}_2 - \mathbf{r}_j) | A \rangle$

Compute thickness function

$$T^{(2)}(b) = \int_{-\infty}^{\infty} dz_1 \int_{-\infty}^{z_1} dz_2 \rho^{(2)}(b_1 = b, z_1; b_2 = b, z_2)$$

Usual approximation

$$\rho^{(2)}(b_1 = b, z_1; b_2 = b, z_2) \approx \rho(b, z_1) \rho(b, z_2)$$

$$T^{(2)}(b) = \frac{1}{2} \left( \int_{-\infty}^{\infty} dz \rho(b, z) \right)^2 = \frac{1}{2} T(b)^2$$

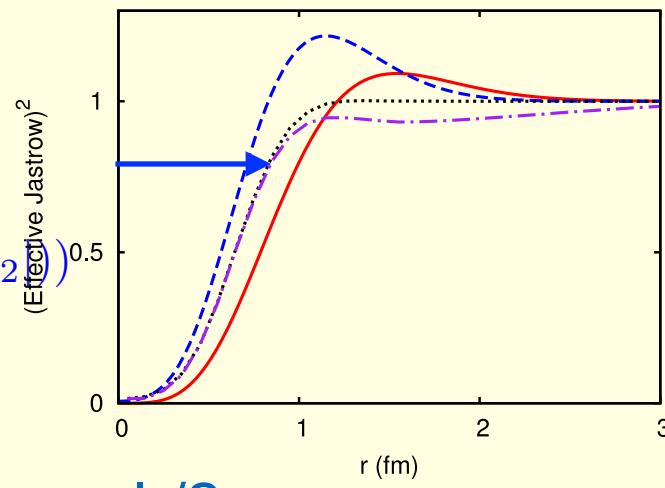
But  $\sim 20\%$  of nucleons are in a correlated pair

$$\rho^{(2)}(b_1 = b, z_1; b_2 = b, z_2) = \rho(b, z_1) \rho(b, z_2) (1 + C(|z_1 - z_2|))$$

$$T^{(2)}(b) \approx T(b)^2 \frac{l_c}{R_A}, \quad l_c = 2 \int_0^{\infty} dz C(z)$$

10-20% reduction depending on nucleus!

Engel, Carlson, Wiringa '11



$l_c/2$

Shadowing effects are overestimated by significant amounts in all approaches that neglect effects of correlations

# Final summary

- EMC effect is related to NN correlations in two theories. Mechanism: PLC suppression enhanced by correlations
- Correlations account for high  $x$  plateau seen in several experiments
- Correlations are important in nuclear shadowing, important for EIC studies of nuclear gluons